

POWER CHAINS IN A DIVISOR GRAPH

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Received: 07 Apr 2019

Accepted: 16 Apr 2019

Published: 27 Apr 2019

ABSTRACT

The divisor graph of an associative ring R (denoted as $DG(R)$) was introduced by Satyanarayana, Srinivasulu.[9]. In this paper, we introduce a simple concept "Power Chain in a Divisor Graph". We prove that if $0 \neq a \in R$ is nilpotent, then the power chain starting with a is of finite length. If $DG(R)$ (the divisor graph of R) contains a power chain starting with $a \in R$ which is of infinite length, then $0 \neq a \neq 1$, a is non-idempotent and non-nilpotent element. We announce some basic results. Finally, we deduce that if R be an integral domain and $a \in R$, then $0 \neq a \neq 1$ if and only if the power chain starting with a (in $DG(R)$) is of infinite length.

KEYWORDS: Associative Ring, Divisor Graph of a Ring, Complete Graph

Mathematics Subject Classification: 05C07, 05C20, 05C76, 05C99, 13E15